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A Thesis presented in partial fulfilment
of the requirements for the degree of
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ALAN L. TYREE
1973

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ABSTRACT

A restricted version of the Tietze Theorem is that
a continuous mapping of a closed subspace of a metric
space ranging in a closed interval may be extended to a
continuous function defined upon the whole metric space.
This may be viewed as a property of the closed interval
and is expressed by saying that the interval is an
absolute extensor. Thus, absolute extensors may be
viewed as a generalisation of real intervals, and many
of the desirable properties of intervals have been
generalised to the class of absolute extensors.

In 1951, Dugundji showed that every convex subset
of a locally convex linear topological space is an
absolute extensor, thus dramatically extending the
Tietze theorem.

In this thesis, a class of subsets of a normed
linear space is defined. This new class of sets includes
the convex sets and it is shown that these new sets are
also absolute extensors.

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