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**Predicting Timber Volume Using
Measurement Error Models and Survey
Sample Theory**

A Thesis presented in partial fulfillment of the requirements
for the degree of

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Stephen Hitchcock

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