

Copyright is owned by the Author of the thesis. Permission is given for a copy to be downloaded by an individual for the purpose of research and private study only. The thesis may not be reproduced elsewhere without the permission of the Author.

# Dealing with Sparsity in Genotype×Environment Analyses

A thesis presented in partial  
fulfilment of the requirements  
for the degree of  
Doctor of Philosophy  
in Statistics

at Massey University,  
Palmerston North, New Zealand.

A. Jonathan R. Godfrey  
2004



**SUPERVISOR'S DECLARATION**

This is to certify that the research carried out for the Doctoral thesis entitled "Dealing with Sparsity in Genotype-by-Environment Analyses" was done by Anthony Jonathan Royce Godfrey in the Institute of Information Sciences and Technology, Massey University, Palmerston North, New Zealand. The thesis material has not been used in part or in whole for any other qualification, and I confirm that the candidate has pursued the course of study in accordance with the requirements of the Massey University regulations.

**Supervisor's Name:** Associate Professor Chin-Diew Lai

**Signature:**

C. D. Lai

**Date:**

2-8-04



**CERTIFICATE OF REGULATORY COMPLIANCE**

This is to certify that the research carried out in the Doctoral Thesis entitled  
**“Dealing with Sparsity in Genotype-by-Environment Analyses”** in the Institute  
of Information Sciences and Technology, Massey University, New Zealand:

- (a) is the original work of the candidate, except as indicated by appropriate attribution in the text and/or in the acknowledgements;
- (b) that the text, excluding appendices/annexes, does not exceed 100,000 words;
- (c) all the ethical requirements applicable to this study have been complied with as required by Massey University, other organisations and/or committees which had particular association with this study, and relevant legislation.

Please insert Ethical Authorisation code(s) here:

N.A.

**Candidate's Name:** Anthony Jonathan Royce Godfrey

**Signature:**

**Date:**

**Supervisor's Name:** Chin-Diew Lai

**Signature:**

**Date:**

2/8/04



**CANDIDATE'S DECLARATION**

This is to certify that the research carried out for my Doctoral thesis entitled "*Dealing with Sparsity in Genotype-by-Environment Analyses*" in the Institute of Information Sciences and Technology, Massey University, Palmerston North, New Zealand, is my own work and that the thesis material has not been used in part or in whole for any other qualification.

**Candidate's Name**

Anthony Jonathan Godfrey

**Signature**

**Date**

02/08/2004

## Abstract

Researchers are frequently faced with the problem of analyzing incomplete and often unbalanced genotype-by-environment ( $G \times E$ ) matrices which arise as a trials programme progresses over seasons. The principal data for this investigation, arising from a ten year programme of onion trials, has less than 2,300 of the 49,200 combinations from the 400 genotypes and 123 environments. This 'sparsity' renders standard  $G \times E$  methodology inapplicable. Analysis of this data to identify onion varieties that suit the shorter, hotter days of tropical and subtropical locations therefore presented a unique challenge.

Removal of some data to form a complete  $G \times E$  matrix wastes information and is consequently undesirable. An incomplete  $G \times E$  matrix can be analyzed using the additive main effects and multiplicative interaction (AMMI) model in conjunction with the EM algorithm but proved unsatisfactory in this instance.

Cluster analysis has been commonly used in  $G \times E$  analyses, but current methods are inadequate when the data matrix is incomplete. If clustering is to be applied to incomplete data sets, one of two routes needs to be taken: either the clustering procedure must be modified to handle the missing data, or the missing entries must be imputed so that standard cluster analysis can be performed.

A new clustering method capable of handling incomplete data has been developed. 'Two-stage clustering', as it has been named, relies on a partitioning of squared Euclidean distance into two independent components, the  $G \times E$  interaction and the genotype main effect. These components are used in the first and second stages of clustering respectively.

Two-stage clustering forms the basis for imputing missing values in a  $G \times E$  matrix, so that a more complete data array is available for other  $G \times E$  analyses. 'Two-stage imputation' estimates unobserved  $G \times E$  yields using inter-genotype similarities to adjust observed yield data in the environment in which the yield is missing. This new imputation method is transferrable to any two-way data situation where all observations are measured on the same scale and the two factors are expected to have significant interaction. This simple, but effective, imputation method is shown to improve on an existing method that confounds the  $G \times E$  interaction and the genotype main effect. Future development of two-stage imputation will use a parameterization of two-stage clustering in a multiple imputation process.

Varieties recommended for use in a certain environment would normally be chosen using results from similar environments. Differing cluster analysis approaches were applied, but led to inconsistent environment clusterings. A graphical summary tool, created to ease the difficulty in identifying the differences between pairs of clusterings, proved especially useful when the number of clusters and clustered observations were high. 'Cluster influence

diagrams' were also used to investigate the effects the new imputation method had on the qualitative structure of the data.

A consequence of the principal data's sparsity was that imputed values were found to be dependent on the existence of observable inter-genotype relationships, rather than the strength of these observable relationships. As a result of this investigation, practical recommendations are provided for limiting the detrimental effects of sparsity. Applying these recommendations will enhance the future ability of two-stage imputation to identify those onion varieties that suit tropical and subtropical locations.

## Acknowledgements

I wish to acknowledge the efforts of many people that have culminated in the submission of this work. First, and foremost, let me thank my supervisors. Professor Graham Wood gave me the opportunity to start a PhD. I will remain eternally grateful for this, the endless supply of advice, kind words, and the occasional kick in the pants that all students need to achieve the best they can. Thanks to Dr Mike Nichols and Dr Ganes Ganesalingam also for their contributions. Other Massey staff have also played a part; Greg Arnold for S-PLUS debugging and advice, Mark Bebbington and Geoff Jones for  $\LaTeX$ commands and debugging, and everyone that came to my seminars and provided feedback over the years.

This work would not have been considered if the real world problem had not existed. Dr Lesley Currah has contributed on numerous occasions with the knowledge surrounding the trials programme. Her patience must at times have worn thin, but it is hoped that she will relish the opportunity that now exists to send our findings to the many collaborators around the world. E-mail has served us well, and the time difference has allowed us each to send well considered questions and responses. Thank you Lesley for everything, including the opportunities for publications, your assistance with proof reading, and generally acting as another supervisor.

There are in fact very many people that need to be remembered for their contributions. I hope each of them receives some joy at the news of the submission of my thesis.

Special mention needs to be paid to those individuals that have assisted in the reading of many papers, document preparation, and all things visually dependent; Zoë Wood, Vince Pegg (for weekends and weeknights), Allister Campbell, Will Samuel, Judy Cann, Graeme Robinson, Michele Bisset, and others.

How can we forget those that ensured that I reached the start of the PhD, and then sustained me through the years. My parents and family have provided the breaks away from Palmerston North that revitalize the spirit; Mum for finishing her PhD first, so that she had time for proof reading. My many flatmates from 1998 to 2002 who put up with my occasional rantings and experimental cooking. The All Blacks and the Black Caps for their various interruptions. Radio Sport for commentaries and the slow paced progress of work over the summer months. The staff at the MUSA shop are yet to vanquish my appetite for apple and cinnamon muffins, let alone the raspberry twists.

Inanimate items serve frequently without thanks. Praise be to the Concise Oxford English Dictionary and various sources of  $\LaTeX$ notes available on the Internet. I have now learned more about the English language and how to present it than I expected at the outset. I thought my command of the language and sentence construction was better than the constant proofing showed me. Sorry to the purists, but I boldly went, and here is the fruit of my labour.

# Contents

<b>Abstract</b>	<b>i</b>
<b>Acknowledgements</b>	<b>iii</b>
<b>Contents</b>	<b>v</b>
<b>List of Figures</b>	<b>ix</b>
<b>List of Tables</b>	<b>xiii</b>
<b>I Background to the Problem</b>	<b>1</b>
<b>1 Setting the scene</b>	<b>3</b>
1.1 Introduction . . . . .	3
1.2 Some key definitions . . . . .	4
1.3 Issues relevant to $G \times E$ research . . . . .	4
1.4 The path to a solution . . . . .	7
1.5 Significance of this investigation . . . . .	10
1.6 Summary . . . . .	11
<b>2 Fundamentals of <math>G \times E</math> analysis</b>	<b>12</b>
2.1 Introduction . . . . .	12
2.2 Establishing the significance of $G \times E$ interaction . . . . .	13
2.3 Joint regression . . . . .	17
2.4 Variations on the joint regression model . . . . .	22
2.5 Multiplicative models . . . . .	26
2.6 Cluster analysis . . . . .	33
2.7 Stability measures . . . . .	39
2.8 Other models and methods . . . . .	46
2.9 Summary . . . . .	51

<b>3</b>	<b>The principal data</b>	<b>52</b>
3.1	Introduction . . . . .	52
3.2	The trials programme . . . . .	52
3.3	The problem of missing data and sparsity . . . . .	57
3.4	Initial data analysis. . . . .	59
3.5	Initial modelling using regression analysis . . . . .	72
3.6	Finding a suitable subset of data . . . . .	77
3.7	Adapting current methodology to allow for incomplete data . . . . .	80
3.8	Analysis with EM-AMMI . . . . .	89
3.9	Summary . . . . .	91
<b>II</b>	<b>Development of a Solution</b>	<b>93</b>
<b>4</b>	<b>Distance measures</b>	<b>95</b>
4.1	Introduction . . . . .	95
4.2	Main effect and interaction distance . . . . .	96
4.3	A partition of Euclidean distance . . . . .	100
4.4	Computation of main effect and interaction distances . . . . .	103
4.5	The metric nature of main effect and interaction distances . . . . .	104
4.6	Estimating unobserved distances . . . . .	107
4.7	A survey of distance measures . . . . .	109
4.8	Comparison of main effect and Euclidean distances . . . . .	114
4.9	Summary . . . . .	119
<b>5</b>	<b>Two-stage clustering</b>	<b>121</b>
5.1	Introduction . . . . .	121
5.2	Description of two-stage clustering . . . . .	124
5.3	An example of two-stage clustering . . . . .	125
5.4	Application of two-stage clustering to the trials programme data . . . . .	129
5.5	Expressing clustering in a parametric model framework . . . . .	138
5.6	Summary . . . . .	142
<b>6</b>	<b>Two-stage imputation</b>	<b>143</b>
6.1	Introduction to imputation of missing data . . . . .	143
6.2	Imputing missing $G \times E$ data . . . . .	147
6.3	An example of two-stage imputation . . . . .	150
6.4	Comprehensive testing of two-stage imputation . . . . .	153
6.5	Application of two-stage imputation to the trials programme data . . . . .	164
6.6	Further ideas for two-stage imputation . . . . .	171
6.7	Summary . . . . .	172

<b>7</b>	<b>Determining mega-environments</b>	<b>173</b>
7.1	Introduction . . . . .	173
7.2	Use of available yield data to cluster environments . . . . .	175
7.3	Use of fully imputed yield data to cluster environments . . . . .	184
7.4	Use of covariates to cluster environments . . . . .	186
7.5	Summary . . . . .	197
<b>8</b>	<b>Comparing cluster analyses</b>	<b>207</b>
8.1	The need to compare cluster analyses . . . . .	207
8.2	Cluster influence diagrams . . . . .	209
8.3	Gauging strength of the relationship between two cluster analyses . . . . .	215
8.4	The consistency of available data . . . . .	218
8.5	The consistency of imputed data . . . . .	223
8.6	The ability of yield data to reflect covariate information . . . . .	230
8.7	The effect of imputation on the $G \times E$ structure . . . . .	235
8.8	The dependence of imputations on commonality of test environments . . . . .	245
8.9	Summary . . . . .	248
<b>III</b>	<b>The Solution: Results and Implications</b>	<b>251</b>
<b>9</b>	<b>Genotype selections for a new environment</b>	<b>253</b>
9.1	Introduction . . . . .	253
9.2	Starting with graphical approaches . . . . .	255
9.3	Genotype selections using stability measures . . . . .	262
9.4	Genotype selections using geographically similar environments . . . . .	271
9.5	Genotype selections using mega-environments . . . . .	273
9.6	Results using partial imputation . . . . .	275
9.7	Summary . . . . .	278
<b>10</b>	<b>Advice for future trials programme designers</b>	<b>280</b>
10.1	Introduction . . . . .	280
10.2	Selection of environments . . . . .	281
10.3	Covariate information . . . . .	285
10.4	Experimental design for individual trials . . . . .	287
10.5	Modelling of planting density . . . . .	291
10.6	Selection of genotypes to include in each environment . . . . .	292
10.7	Enhancing the connectedness of the $G \times E$ matrix . . . . .	298
10.8	Summary . . . . .	306

<b>11 Conclusion</b>	<b>309</b>
11.1 Introduction . . . . .	309
11.2 Background to the investigation . . . . .	309
11.3 New theoretical developments . . . . .	312
11.4 Implications and recommendations arising from the investigation . . . . .	315
11.5 Summary . . . . .	317
<b>A Data from the Onion Trials Programme</b>	<b>318</b>
<b>B References</b>	<b>330</b>

# List of Figures

1.1	Flow chart depicting the solution path . . . . .	8
2.1	Alternative representation of Finlay and Wilkinson (1963) plot of genotype stability and mean yield . . . . .	21
3.1	Genotype means, standard deviations, and the number of times each was used plotted against one another . . . . .	60
3.2	Environment means, standard deviations, and the number of times each was used plotted against one another . . . . .	61
3.3	Normal probability plots for yield . . . . .	63
3.4	Genotype means, standard deviations, and the number of times each was used plotted against one another (using square roots of yield) . . . . .	64
3.5	Environment means, standard deviations, and the number of times each was used plotted against one another (using square roots of yield) . . . . .	65
3.6	Diagnostic plots of environment altitudes and latitudes . . . . .	66
3.7	Onion yields plotted against altitude and latitude . . . . .	67
3.8	Square root of yield plotted against altitude and latitude . . . . .	68
3.9	Environmental means and standard deviations of square roots of yields plotted against latitudes and altitudes . . . . .	69
3.10	Yields of Red Synthetic HZ plotted against environment altitude and latitude	70
3.11	Relative yields of Red Synthetic HZ plotted against environment altitude and latitude . . . . .	71
3.12	Range of growing periods plotted against median of growing periods for environments . . . . .	72
3.13	Medians and ranges of growing periods plotted against latitude . . . . .	73
3.14	Diagnostic plots for the best regression model for yield . . . . .	76
3.15	Comparison of adjusted coefficients of variation for 87 genotypes . . . . .	82
3.16	Histograms of adjusted superiority scores for Onion Data I and II . . . . .	86
3.17	Plots of adjusted superiority measures versus genotype usage . . . . .	88
4.1	Two pairs of genotypes showing the difference between shape and level similarity . . . . .	98

4.2	Graphical representation of the partition of Euclidean distance for two genotypes in two environments . . . . .	102
4.3	Diagram illustrating shortest path concept . . . . .	108
4.4	Expected value of main effect and Euclidean distance . . . . .	117
4.5	Mean squared error of main effect and Euclidean distance . . . . .	118
5.1	An example of first stage clustering of complete data . . . . .	126
5.2	An example of first stage clustering of incomplete data . . . . .	127
5.3	An example of second stage clustering of incomplete data . . . . .	128
5.4	Effects of using within-environment standardization on Onion Data I . . . .	130
5.5	Effects of using within-environment standardization on Onion Data II . . .	131
5.6	Effects of using within-environment standardization on the square roots of Onion Data I yields . . . . .	132
5.7	Effects of using within-environment standardization on the square roots of Onion Data II yields . . . . .	133
5.8	First stage clustering of genotypes from Onion Data I . . . . .	134
5.9	First stage clustering of genotypes from Onion Data II . . . . .	136
5.10	Two-stage clustering of a first stage cluster from Onion Data I . . . . .	139
5.11	Two-stage clustering of a first stage cluster from Onion Data II . . . . .	140
6.1	Yields of three genotypes plotted over six environments to illustrate imputation strategies . . . . .	149
6.2	Clustering of 58 genotypes using Euclidean distance of Ouyang <i>et al.</i> (1995)	152
6.3	Yields of three similar genotypes plotted against an environmental index to illustrate imputation results . . . . .	152
6.4	Boxplots of yields versus environments for Fox and Rathjen (1981) data . .	155
6.5	Histograms of range standardized imputed yields for Onion Data I and II .	165
6.6	Within environment correlation of fully imputed Onion Data I and II plotted against environment usage . . . . .	167
6.7	Dendrogram of Onion Data I genotypes, clustered using interaction distance applied to two-stage imputed data . . . . .	167
6.8	Dendrogram of Onion Data II genotypes, clustered using interaction distance applied to two-stage imputed data . . . . .	168
6.9	Dendrogram of Onion Data I genotypes, clustered using Euclidean distance applied to incomplete data . . . . .	169
6.10	Dendrogram of Onion Data II genotypes, clustered using Euclidean distance applied to incomplete data . . . . .	169
6.11	Dendrogram of Onion Data I genotypes, clustered using Euclidean distance applied to nearest cluster imputed data . . . . .	170

6.12	Dendrogram of Onion Data II genotypes, clustered using Euclidean distance applied to nearest cluster imputed data . . . . .	170
7.1	Histograms of within-genotype standardized yields. . . . .	176
7.2	Histograms of within-genotype standardized square roots of yields. . . . .	178
7.3	Dendrogram of all 123 environments of the Onion Trials Programme clustered using incomplete data . . . . .	179
7.4	Dendrogram of 109 Onion Data I environments clustered using incomplete data . . . . .	179
7.5	Dendrogram of the 98 Onion Data II environments clustered using incomplete data . . . . .	181
7.6	Genotype standard deviations plotted against means for Onion Data I and II after two-stage imputation . . . . .	184
7.7	Effects on within-environment standard deviations and means of the within-genotype standardization . . . . .	185
7.8	Dendrogram of 109 Onion Data I environments based on two-stage imputed yields . . . . .	186
7.9	Dendrogram of 98 Onion Data II environments based on two-stage imputed yields . . . . .	189
7.10	Heat unit variables plotted against one another . . . . .	193
7.11	Photoperiod variables plotted against one another . . . . .	194
7.12	Normal probability plots and boxplots of transformed proxy variables . . . . .	198
7.13	Dendrogram of 101 environments clustered using proxy variables . . . . .	199
7.14	Normal probability plots and boxplots of transformed covariates . . . . .	201
7.15	Normal probability plots and boxplots of transformed covariates . . . . .	202
7.16	Dendrogram of 89 environments clustered using proxy variables . . . . .	203
7.17	Dendrogram of 79 environments clustered using constructed covariates . . . . .	205
8.1	Cluster influence diagram for dendrograms of Figures 7.16 and 7.17 . . . . .	210
8.2	Cluster influence diagram for dendrograms in Figures 7.13 and 7.16 . . . . .	212
8.3	Cluster influence diagram for dendrograms in Figures 7.13 and 7.17 . . . . .	213
8.4	Cluster influence diagram for dendrograms in Figures 7.3 and 7.4 . . . . .	219
8.5	Cluster influence diagram for dendrograms in Figures 7.4 and 7.5 . . . . .	220
8.6	Cluster influence diagram for dendrograms in Figures 7.3 and 7.5 . . . . .	221
8.7	Cluster influence diagram for dendrograms in Figures 7.4 and 7.8 . . . . .	225
8.8	Cluster influence diagram for dendrograms in Figures 7.5 and 7.9 . . . . .	226
8.9	Cluster influence diagram for dendrograms in Figures 7.8 and 7.9 . . . . .	228
8.10	Cluster influence diagram for dendrograms in Figures 6.7 and 6.8 . . . . .	229
8.11	Cluster influence diagram for dendrograms in Figures 7.3 and 7.13 . . . . .	231
8.12	Cluster influence diagram for dendrograms in Figures 7.4 and 7.16 . . . . .	233

8.13	Cluster influence diagram for dendrograms in Figures 7.5 and 7.17 . . . . .	234
8.14	Cluster influence diagram for dendrograms in Figures 7.8 and 7.16 . . . . .	236
8.15	Cluster influence diagram for dendrograms in Figures 7.9 and 7.17 . . . . .	237
8.16	Effects of nearest cluster imputation on clustering of genotypes in Onion Data I . . . . .	239
8.17	Effects of nearest cluster imputation on clustering of genotypes in Onion Data II . . . . .	240
8.18	Effects of two-stage imputation on clustering of genotypes in Onion Data I	242
8.19	Effects of two-stage imputation on clustering of genotypes in Onion Data II	243
9.1	Correlation of latitude and expected yield plotted against mean yield . . . .	256
9.2	Biplot of first and second interaction axes for Onion Data I . . . . .	257
9.3	Biplot of first and second interaction axes for Onion Data II . . . . .	258
9.4	Scree plots for principal component contributions to Onion Data I and II .	260
9.5	Histograms of Wricke's ecovalences for Onion Data I and II . . . . .	266
9.6	Histograms of adjusted Lin and Binns superiority scores for Onion Data I and II . . . . .	270
9.7	Average relative performances of genotypes over geographically similar en- vironments . . . . .	273
9.8	Average relative performances of genotypes over environments within a mega-environment . . . . .	275
10.1	Inter-genotype connectedness of Onion Data II . . . . .	300
10.2	Inter-environment connectedness of Onion Data II . . . . .	301
10.3	Flow chart showing the suggested method for selecting genotypes for a new trial . . . . .	305

# List of Tables

2.1	Summary of stability statistics . . . . .	40
2.2	A second summary of stability statistics . . . . .	41
3.1	Models used to explain yield performance . . . . .	74
3.2	Summary of various regression models fitted to the sparse Onion Trials Programme data . . . . .	75
3.3	ANOVA for the best regression model for yield . . . . .	76
3.4	Partial ANOVA specific to the most commonly tested genotype of the Onion Trials Programme . . . . .	77
3.5	Effects of data deletion on principal data. . . . .	78
3.6	Genotypes with a high adjusted coefficient of variation . . . . .	81
3.7	Genotypes with high contribution to $G \times E$ interaction . . . . .	84
3.8	Genotypes selected using the adjusted superiority score . . . . .	85
3.9	Six onion varieties that were successful in the single Trial where they were tested . . . . .	87
3.10	Correlations of fitted values from a series of EM-AMMI models . . . . .	89
3.11	Number of iterations taken to fit EM-AMMI models, and correlation of results between data sets . . . . .	89
3.12	Unrealistic yields found using various EM-AMMI models . . . . .	90
3.13	Effects of using an alternative set of starting values for EM-AMMI models . . . . .	90
5.1	Fifteen $G \times E$ combinations randomly deleted to create an incomplete set of data. . . . .	127
5.2	Comparison of cluster memberships for complete and incomplete data . . . . .	127
5.3	Cluster memberships for the first stage clustering of Onion Data I genotypes	135
5.4	Cluster memberships for the first stage clustering of Onion Data II genotypes	137
6.1	Imputed values found for fifteen deleted observations . . . . .	151
6.2	Summary details of the data sets used in simulation testing . . . . .	154
6.3	Comparison of all pairs of imputation methods (raw data). . . . .	157
6.3	<i>continued</i> . . . . .	158

6.4	Comparison of all pairs of imputation methods (within-environment standardized data) . . . . .	159
6.4	<i>continued</i> . . . . .	160
6.5	Correlations of imputed values and deleted values (raw data) . . . . .	162
6.6	Correlations of imputed values and deleted values (within-environment standardized data) . . . . .	163
6.7	Details of Onion Data I and II imputed values trimmed during imputation .	165
7.1	Cluster memberships for the dendrogram presented in Figure 7.3 . . . . .	180
7.1	<i>continued</i> . . . . .	181
7.2	Cluster memberships for the dendrogram presented in Figure 7.4 . . . . .	182
7.3	Cluster memberships for the dendrogram presented in Figure 7.5 . . . . .	183
7.4	Cluster memberships for the dendrogram presented in Figure 7.8 . . . . .	187
7.5	Cluster memberships for the dendrogram presented in Figure 7.9 . . . . .	188
7.6	Correlations of proxy variables for environments . . . . .	192
7.7	Summary of regression models for proxy variables using latitude and altitude as explanatory variables . . . . .	195
7.8	Summary of best subsets regression of latitude and altitude on proxy variables	196
7.9	Cluster memberships for the dendrogram presented in Figure 7.13 . . . . .	200
7.10	Cluster memberships for the dendrogram presented in Figure 7.16 . . . . .	204
7.11	Cluster memberships for the dendrogram presented in Figure 7.17 . . . . .	206
8.1	Numerical summary statistics for Figures 8.1, 8.2, and 8.3 . . . . .	217
8.2	Numerical summary statistics for Figures 8.4, 8.5, and 8.6 . . . . .	222
8.3	Numerical summary statistics for Figures 8.7 and 8.8 . . . . .	224
8.4	Numerical summary statistics for Figures 8.9 and 8.10 . . . . .	227
8.5	Numerical summary statistics for Figures 8.11 to 8.15 . . . . .	232
8.6	Summary statistics that quantify effects of imputation methods on clustering of genotypes . . . . .	241
8.7	Number of genotype clusters found using sparse and imputed data . . . . .	244
8.8	Complete table of numerical summary statistics to support all cluster influence diagrams of Chapter 8 . . . . .	246
8.9	$\lambda$ and $U$ coefficients for clustering of genotypes based on imputed data and commonality of test environments . . . . .	247
9.1	Details of twelve environments with covariate data, but not used in imputations . . . . .	254
9.2	Genotypes with high specific adaptation to low latitude environments . . .	256
9.3	Genotype codes used in the biplots of Figures 9.2 and 9.3 . . . . .	259

9.4	Partial ANOVA for various AMMI models applied to imputed yields of Onion Data I . . . . .	261
9.5	Partial ANOVA for various AMMI models applied to imputed yields of Onion Data II . . . . .	262
9.6	Genotype selections chosen using the adjusted coefficient of variation . . . . .	264
9.7	Genotype selections chosen using Wricke's ecovalence . . . . .	265
9.8	Genotype selections chosen using adjusted superiority scores . . . . .	267
9.9	Check variety selections for Onion Data I using two nonparametric stability measures . . . . .	268
9.10	Check variety selections for Onion Data II using two nonparametric stability measures . . . . .	268
9.11	Check variety selections for Onion Data I using two more nonparametric stability measures . . . . .	269
9.12	Check variety selections for Onion Data II using two more nonparametric stability measures . . . . .	269
9.13	Correlations of wide adaptation stability measures . . . . .	271
9.14	Genotypes selected on their success in geographically similar environments . . . . .	272
9.15	Genotypes selected on their success in environments within the same mega- environment . . . . .	274
9.16	Genotypes not given estimated performances in the new trial when using partial imputation . . . . .	276
9.17	Genotype selections for the new Yemeni trial, based on partially imputed Onion Data I and II $G \times E$ matrices . . . . .	277
10.1	Covariate genotype information recommended for collection . . . . .	285
10.2	Covariate environment information recommended for collection . . . . .	286
10.3	Additional covariate information recommended for collection during new trials in the Onion Trials Programme . . . . .	286
10.4	Genotype pairs whose linkage would be enhanced by the suggested new trial . . . . .	302
10.5	A portion of the concurrence matrix for Onion Data I . . . . .	304
A.1	Names of varieties used in core data sets . . . . .	319
A.1	<i>continued</i> . . . . .	320
A.2	Genotypes not included in Onion Data I or II . . . . .	321
A.2	<i>continued</i> . . . . .	322
A.3	Codes for trials included in Onion Data I and II . . . . .	323
A.4	Summary information for environments . . . . .	324
A.4	<i>continued</i> . . . . .	325
A.4	<i>continued</i> . . . . .	326
A.5	Artificial covariates used in environmental clustering . . . . .	327

A.5 <i>continued</i> . . . . .	328
A.5 <i>continued</i> . . . . .	329